Polynomials

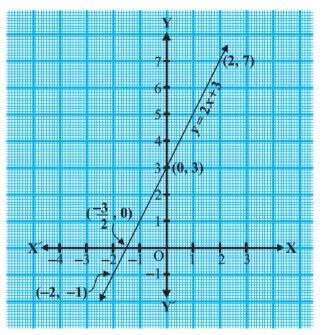
• If p(x) is a polynomial in x, the highest power of x in p(x) is called the degree of the polynomial p(x).

Types of Polynomials

- A polynomial of degree 1 is called a linear polynomial.
- A polynomial of degree 2 is called a quadratic polynomial.
- A polynomial of degree 3 is called a cubic polynomial.

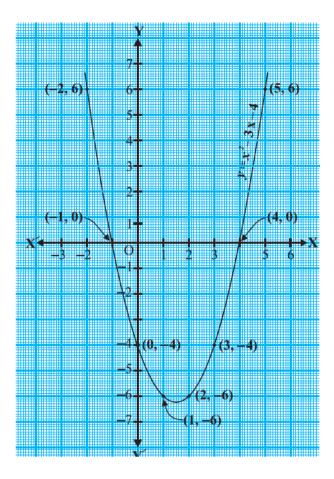
Zeroes of a Polynomial

- If p(x) is a polynomial in x, and if k is any real number, then the value obtained by replacing x by k in p(x), is called the value of p(x) at x = k, and is denoted by p(k).
- A real number k is said to be a zero of a polynomial p(x), if p(k) = 0.
- Geometrical Meaning of Zeroes of Polynomials

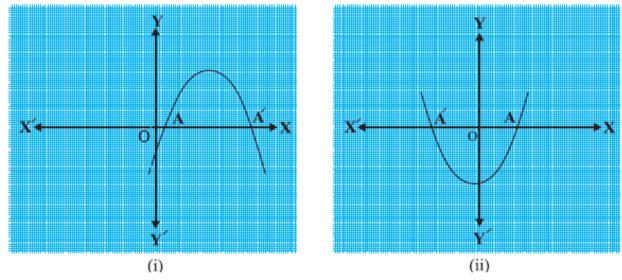






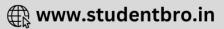


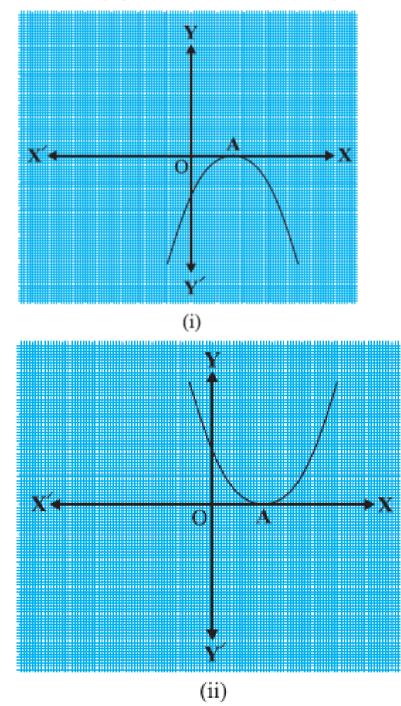
• The equation $ax^2 + bx + c$ can have three cases for the graphs



• Case (i): Here, the graph cuts x-axis at two distinct points A and A'.







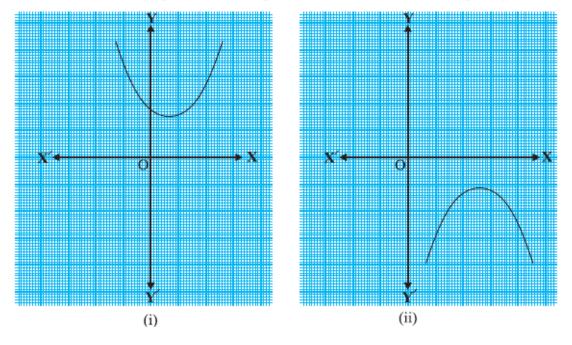
Case (ii): Here, the graph cuts the x-axis at exactly one point

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Case (iii): Here, the graph is either completely above the x-axis or completely below the x-axis.



Relationship between Zeroes and Coefficients of a Polynomial

If α and β are the zeroes of the quadratic polynomial $p(x) = ax^2 + bx + c$, $a \neq 0$, then you know that $x - \alpha$ and $x - \beta$ are the factors of p(x). $A + \beta = -b/a$ $\alpha\beta = c/a$

Division Algorithm for Polynomials

- If p(x) and g(x) are any two polynomials with g(x) ≠ 0, then we can find polynomials q(x) and r(x) such that p (x) = g(x) × q(x) + r(x), where r(x) = 0 or degree of r(x) < degree of g(x). This result is known as the Division Algorithm for polynomials.
 Consider the cubic polynomial x³ 3x² x + 3. If one of its zeroes is 1, then x 1 is a factor of x³ 3x² x + 3.
- So, you can divide $x^3 3x^2 x + 3$ by x 1, Next, you could get the factors of $x^2 - 2x - 3$, by splitting the middle term, as: (x + 1) (x - 3). This would give you: $x^3 - 3x^2 - x + 3 = (x - 1) (x^2 - 2x - 3)$ = (x - 1) (x + 1) (x - 3)So, all the three zeroes of the cubic polynomial are now known to you as 1, -1, 3.

